

CHAPTER 2

**Problem 2-1**

Line Voltage = 460 V, Resistance = 8.66 ohm

Reactance = 5 ohm

Reference voltage =  $\hat{v}_{an} = 265.6 + j0$

(a) The line current

= phase current since wye connected

$$= (265.6 + j0) / (8.66 + j5)$$

$$= 23.0 - j13.28 = 26.56 \angle -30^\circ$$

(b) Total power =  $3 \times 26.56^2 \times 8.66 = 18\,325.4 \text{ W}$

(c) The two wattmeter readings are:

Wattmeter in line B:

$$\hat{v}_{ba} = 460 \angle -150^\circ$$

$$\hat{i}_b = 26.56 \angle -150^\circ$$

$$P_b = 460 \times 26.56 \times \cos(0)$$

$$= 12\,217$$

Wattmeter in line C:

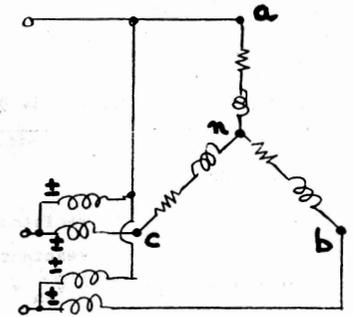
$$\hat{v}_{ca} = 460 \angle 150^\circ$$

$$\hat{i}_c = 26.56 \angle 90^\circ$$

$$P_c = 460 \times 26.56 \times \cos(60)$$

$$= 6108.4$$

Sum of the two readings = 18 325.4 W



**Problem 2-2**

Line Voltage = 460 V, Resistance = 8.66 ohm

Reactance = 5.00 ohm

Reference voltage =  $\hat{v}_{ab} = 460 + j0$

(a) Phase current =  $(460 + j0) / (8.66 + j5)$

$$= 39.84 - j23.00 = 46.00 \angle -30^\circ$$

$$\text{Line current} = 79.68 \angle -60^\circ$$

(b) Total power =  $3 \times 46.00^2 \times 8.66 = 54\,976.1 \text{ W}$

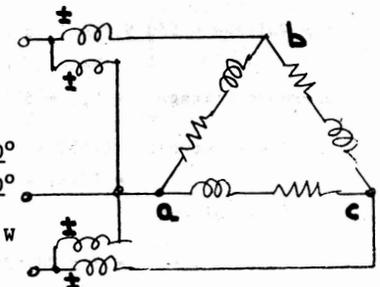
(c) The two wattmeter readings are:

Wattmeter in line B:

$$\hat{v}_{ba} = 460 \angle 180^\circ$$

Wattmeter in line C:

$$\hat{v}_{ca} = 460 \angle 120^\circ$$



**Problem 2-10**

Line Voltage 208

$$\begin{aligned} \hat{Z}_{ba} &= (10 + j20) = 22.36 \angle 63.43^\circ \\ \hat{Z}_{cb} &= (20 - j10) = 22.36 \angle -26.57^\circ \\ \hat{Z}_{ac} &= (20 + j10) = 22.36 \angle 26.57^\circ \end{aligned}$$

Reference Voltage =  $\hat{V}_{ac} = 208 + j0$

(a) The phase voltages are:

$$\begin{aligned} \hat{V}_{ac} &= 208 + j0 \\ \hat{V}_{cb} &= 208 \angle -120^\circ = -104 - j180.1 \\ \hat{V}_{ba} &= 208 \angle +120^\circ = -104 + j180.1 \end{aligned}$$

(b) The phase currents are:

$$\begin{aligned} \hat{I}_{ac} &= (208 + j0) / (20 + j10) = 8.32 - j4.16 \\ &= 9.3 \angle -26.57^\circ \\ \hat{I}_{cb} &= (-104 - j180.1) / (20 - j10) = -0.558 - j9.284 \\ &= 9.3 \angle -93.44^\circ \\ \hat{I}_{ba} &= (-104 + j180.1) / (10 + j20) = 5.125 + j7.762 \\ &= 9.3 \angle 56.57^\circ \end{aligned}$$

(c) The line currents are:

$$\begin{aligned} \hat{I}_a &= (8.32 - j4.16) - (5.125 + j7.762) = 3.195 - j11.922 \\ &= 12.343 \angle -75.00^\circ \\ \hat{I}_b &= (5.125 + j7.762) - (-0.558 - j9.284) = 5.683 + j17.046 \\ &= 17.97 \angle 71.56^\circ \\ \hat{I}_c &= (-0.558 - j9.284) - (8.32 - j4.16) = 8.878 - j5.124 \\ &= 10.251 \angle -150.00^\circ \end{aligned}$$

(d) Two-wattmeter readings:

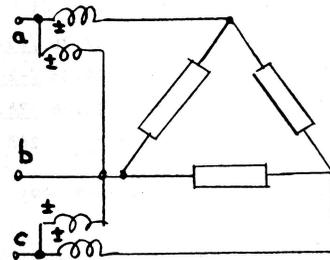
Wattmeter in line C:

$$\begin{aligned} \hat{V}_{cb} &= 208 \angle -120^\circ \\ \hat{I}_c &= 10.251 \angle -150^\circ \\ P_c &= 208 \times 10.251 \times \cos(30) \\ &= 1846.55 \end{aligned}$$

Wattmeter in line A:

$$\begin{aligned} \hat{V}_{ab} &= 208 \text{ at } \angle -60^\circ \\ \hat{I}_a &= 12.343 \angle -75.00^\circ \\ P_a &= 208 \times 12.343 \times \cos(15) \\ &= 2479.86 \end{aligned}$$

Sum of the 2 readings = 4326.4 W



(e) The phase powers:

$$\begin{aligned} P_{ac} &= 9.3^2 \times 20 = 1730.56 \text{ W} \\ P_{cb} &= 9.3^2 \times 20 = 1730.56 \text{ W} \\ P_{ba} &= 9.3^2 \times 10 = 865.28 \text{ W} \\ \text{Sum} &= 4326.40 \text{ W} \end{aligned}$$

**Problem 2-11**

Line Voltage = 460 V

$$\begin{aligned} \hat{Z}_{ab} &= (25 + j15) = 29.15 \angle 30.96^\circ \\ \hat{Z}_{bc} &= (15 - j25) = 29.15 \angle -59.04^\circ \\ \hat{Z}_{ca} &= (20 + j20) = 28.28 \angle 45^\circ \end{aligned}$$

Reference voltage =  $\hat{V}_{ab} = 460 \angle 0^\circ$

(a) The phase voltages are:

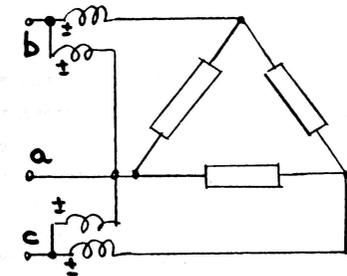
$$\begin{aligned} \hat{V}_{ab} &= 460 \angle 0^\circ = 460 + j0 \\ \hat{V}_{bc} &= 460 \angle -120^\circ = -230 - j398.37 \\ \hat{V}_{ca} &= 460 \angle +120^\circ = -230 + j398.37 \end{aligned}$$

(b) The phase currents are:

$$\begin{aligned} \hat{I}_{ab} &= (460 + j0) / (25 + j15) = 13.529 - j8.118 \\ &= 15.78 \angle -30.96^\circ \\ \hat{I}_{bc} &= (-230 - j398.37) / (15 - j25) = 7.658 - j13.795 \\ &= 15.78 \angle -60.96^\circ \\ \hat{I}_{ca} &= (-230 + j398.37) / (20 + j20) = 4.209 + j15.709 \\ &= 16.26 \angle 75^\circ \end{aligned}$$

(c) The line currents are:

$$\begin{aligned} \hat{I}_a &= (13.529 - j8.118) - (4.209 + j15.709) = 9.32 - j23.827 \\ &= 25.585 \angle -68.64^\circ \\ \hat{I}_b &= (7.658 - j13.795) - (13.529 - j8.118) = -5.871 - j5.667 \\ &= 8.167 \angle -135.96^\circ \\ \hat{I}_c &= (4.209 + j15.709) - (7.658 - j13.795) = -3.448 + j29.504 \\ &= 29.705 \angle 96.67^\circ \end{aligned}$$





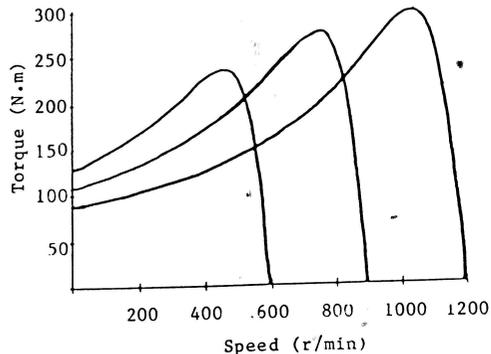
Problem 7-19

$V_t = 440$  V,  $f = 60$  Hz, Poles = 6, Delta connection  
 $R_1 = 1.5$  ohm,  $R_2' = 0.8$  ohm  
 Stator leakage inductance = 0.008 H, Rotor leakage inductance = 0.008 H  
 Magnetizing inductance = 0.3 H, Turns ratio = 1

Approximate equivalent

$X_1 = 3.016$ ,  $X_2' = 3.016$ ,  $X_m = 113.1$  ohm at 60 Hz

- (a) This is a repeat of Prob. 7-18
- (b) Repeat Prob 7-18 with  $X_1 = 2.262$ ,  $X_2' = 2.262$ ,  $X_m = 84.8$  ohm at 45 Hz  
 $V_{ph} = 0.75 \times 440 = 330$  V
- (c) Repeat Prob 7-18 with  $X_1 = 1.508$ ,  $X_2' = 1.508$ ,  $X_m = 56.55$  ohm at 30 Hz  
 $V_{ph} = 0.5 \times 440 = 220$  V



(d) The maximum torques are

f (Hz)	$T_m$ (N.m)	Speed (r/min)	Slip
60	300	1045	0.19
45	275	750	0.17
30	235	460	0.24

Note:  $T_m$  is reduced as the frequency is reduced since  $R_1$  is not neglected.

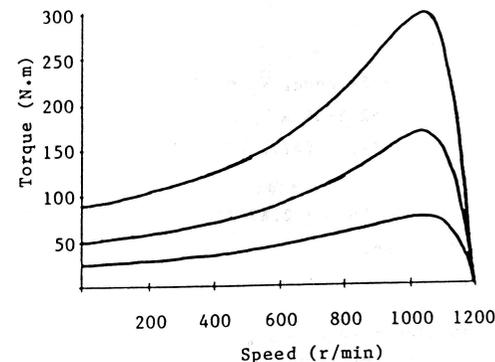
Problem 7-20

$V_t = 440$  V,  $f = 60$  Hz, Poles = 6, Delta connection  
 $R_1 = 1.5$  ohm,  $R_2' = 0.8$  ohm  
 Stator leakage inductance = 0.008 H, Rotor leakage inductance = 0.008 H  
 Magnetizing inductance = 0.3 H, Turns ratio = 1

Approximate equivalent

$X_1 = 3.016$ ,  $X_2' = 3.016$ ,  $X_m = 113.1$  ohm at 60 Hz

- (a) This is a repeat of Prob. 7-18
- (b) Repeat 7-18 with  $V_{ph} = 330$  V
- (c) Repeat 7-18 with  $V_{ph} = 220$  V



(d) The maximum torques are:

Voltage (V)	$T_m$ (N.m)	Speed (r/min)	Slip
440	300	1045	0.19
330	170	1045	0.19
220	75	1045	0.19

**Problem 8-10**

$V_t = 550$  V,  $f = 60$  Hz, Poles = 10, Wye connection

$X_s = 2.9$  ohm/ph,  $R_a = 0$

Power = 75 kW, Power factor = 1.0, Increase in  $I_f = 20\%$

(a) Taking  $\hat{V}_t$  (phase) as reference,  $\hat{V}_t = 317.54 + j0$

$$I_a = \frac{75 \times 1000}{1.7321 \times 550 \times 1} = 78.73$$

$$\hat{I}_a = 78.73 + j0$$

$$\hat{E}_f = (317.54 + j0) - (78.73 + j0) (j2.9) = 317.5426 - j228.316$$

$$= 391.10 \angle -35.72^\circ \text{ V (phase)}$$

$$E_f = 677.41 \text{ V (line)}$$

(b)  $I_r =$  component of  $\hat{I}_a$  in phase with  $\hat{V}_t$   
 $= 78.73$  A (constant)

$$E_f = 391.10 \times 1.2 = 469.328$$

$$\text{Im}[\hat{E}_f] = -228.316 \text{ (constant)}$$

$$\text{Re}[\hat{E}_f] = \sqrt{(469.328^2 - 228.316^2)} = 410.04$$

$$\text{That is, } \hat{E}_f = 410.04 - j228.32 = 469.328 \angle -29.11^\circ \text{ V}$$

$$\text{But } \hat{V}_t = 317.54 + j0$$

$$j\hat{I}_a X_s = (317.54 + j0) - (410.04 - j228.32) = -92.50 + j228.32$$

$$= 246.34 \angle 112.06^\circ \text{ V}$$

$$\hat{I}_a = 84.95 \angle 22.06^\circ \text{ A}$$

$$\text{Increase in } I_a = (84.95 - 78.73) / 78.73 = 7.90\%$$

**Problem 8-11**

$V_t = 460$  V,  $f = 60$  Hz, Poles = 10, Wye connection

$X_s = 2.5$  ohm/ph,  $R_a = 0$

Power = 60 kW, Power factor = 1.0, Increase in  $I_f = 25\%$

(a) Taking  $\hat{V}_t$  (phase) as reference,  $\hat{V}_t = 265.58 + j0$

$$I_a = \frac{60 \times 1000}{1.732 \times 460 \times 1} = 75.31 \text{ A}$$

$$\hat{I}_a = 75.31 + j0$$

$$\hat{E}_f = (265.58 + j0) - (75.31 + j0) (j2.5) = 265.5811 - 188.266$$

$$= 325.54 \angle -35.33^\circ \text{ V (phase)}$$

$$E_f = 563.86 \text{ V (line)}$$

(b)  $I_r =$  component of  $\hat{I}_a$  in phase with  $\hat{V}_t$   
 $= 75.31$

$$E_f = 325.54 \times 1.25 = 406.93 \text{ V}$$

$$\text{Im}[\hat{E}_f] = -188.27$$

$$\text{Re}[\hat{E}_f] = \sqrt{(406.93^2 - 188.27^2)} = 360.76$$

$$\hat{E}_f = 360.76 - j188.27 = 406.93 \angle -27.56^\circ$$

$$\hat{V}_t = 265.58 + j0$$

$$j\hat{I}_a X_s = (265.58 + j0) - (360.76 - j188.27)$$

$$= -95.18 + j188.27 = 210.96 \angle 116.82^\circ \text{ V}$$

$$\hat{I}_a = 84.38 \angle 26.82^\circ \text{ A}$$

$$\text{Increase in } I_a = (84.38 - 75.31) / 75.31 = 12.05\%$$

**Problem 8-12**

$V_t = 460$  V,  $f = 60$  Hz, Poles = 10, Wye connection

$X_s = 0.8$  ohm/ph,  $R_a = 0$

Power = 200 kW, Power factor = 0.8 (leading), Increase in torque = 100%

(a) Taking  $\hat{V}_t$  (phase) as reference,  $\hat{V}_t = 265.58 + j0$

$$I_a = \frac{200 \times 1000}{1.7321 \times 460 \times 0.8} = 313.78 \text{ A}$$

$$\hat{I}_a = 313.78 (0.8 + j0.6) = 251.0264 + j188.2664$$

$$\hat{E}_f = (265.58 + j0) - (251.0264 + j188.2664) (j0.8) = 416.1942 - j200.817$$

$$= 462.11 \angle -25.76^\circ \text{ V (phase)}$$

$$E_f = 800.40 \text{ V (line)}$$

(b)  $I_r =$  component of  $\hat{I}_a$  in phase with  $\hat{V}_t$   
 $= 251.0264 \times 2 = 502.0528 \text{ A}$

$$E_f = 462.11 \text{ V (constant)}$$

$$\text{Im}[\hat{E}_f] = -502.0528 \times 0.8 = -401.63 \text{ V}$$

$$\text{Re}[\hat{E}_f] = \sqrt{(462.11^2 - 401.63^2)} = 228.55 \text{ V}$$

$$\hat{E}_f = 228.55 - j401.63$$

$$\hat{V}_t = (265.58 + j0)$$