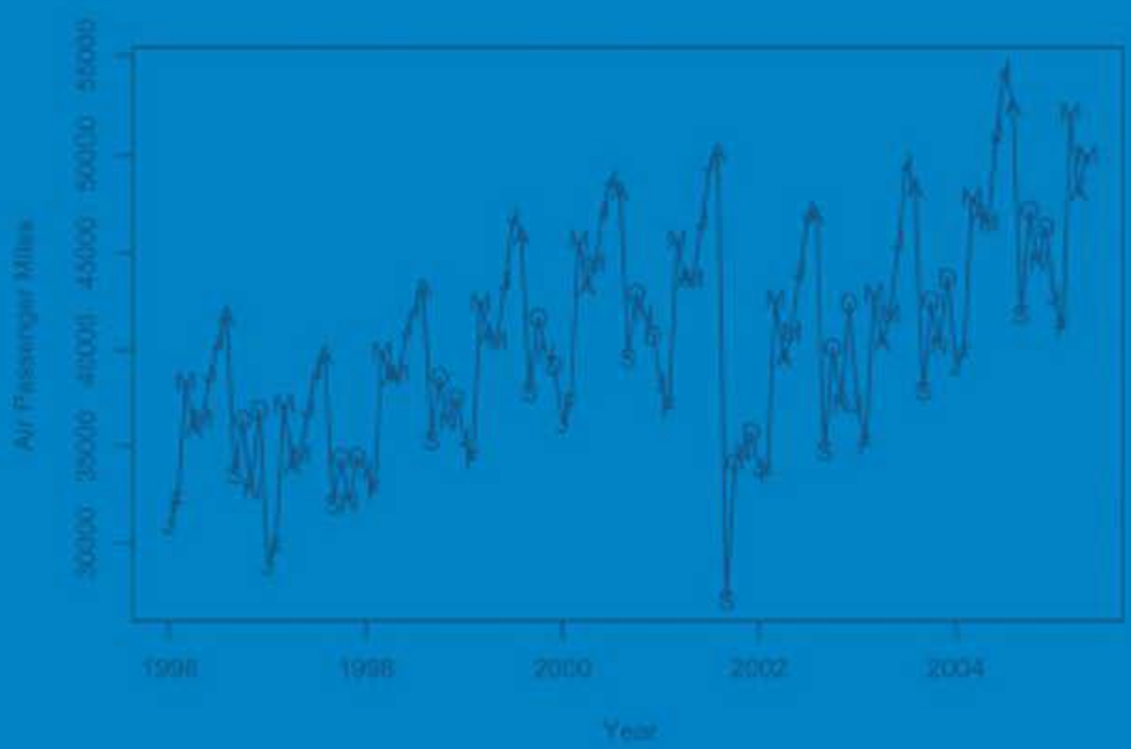
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PREFACE

The theory and practice of time series analysis have developed rapidly since the appearance in 1970 of the seminal work of George E. P. Box and Gwilym M. Jenkins, *Time Series Analysis: Forecasting and Control*, now available in its third edition (1994) with co-author Gregory C. Reinsel. Many books on time series have appeared since then, but some of them give too little practical application, while others give too little theoretical background. This book attempts to present both application, and theory at a level accessible to a wide variety of students and practitioners. Our approach is to mix application and theory throughout the book as they are naturally needed.

The book was developed for a one-semester course usually attended by students in statistics, economics, business, engineering, and quantitative social sciences. Basic applied statistics through multiple linear regression is assumed. Calculus is assumed only to the extent of minimizing sums of squares, but a calculus-based introduction to statistics is necessary for a thorough understanding of some of the theory. However, required facts concerning expectation, variance, covariance, and correlation are reviewed in appendices. Also, conditional expectation properties and minimum mean square error prediction are developed in appendices. Actual time series data drawn from various disciplines are used throughout the book to illustrate the methodology. The book contains additional topics of a more advanced nature that can be selected for inclusion in a course if the instructor so chooses.

All of the plots and numerical output displayed in the book have been produced with the R software, which is available from the R Project for Statistical Computing at www.r-project.org. Some of the numerical output has been edited for additional clarity or for simplicity. R is available as free software under the terms of the Free Software Foundation's GNU General Public License in source code form. It runs on a wide variety of UNIX platforms and similar systems, Windows, and MacOS.

R is a language and environment for statistical computing and graphics, provides a wide variety of statistical (e.g., time-series analysis, linear and nonlinear modeling, classical statistical tests) and graphical techniques, and is highly extensible. The extensive appendix An Introduction to R, provides an introduction to the R software specially designed to go with this book. One of the authors (KSC) has produced a large number of new or enhanced R functions specifically tailored to the methods described in this book. They are listed on page 468 and are available in the package named TSA on the R Project's Website at www.r-project.org. We have also constructed R command script files for each chapter. These are available for download at www.stat.uiowa.edu/~kchan/TSA.htm. We also show the required R code beneath nearly every table and graphical display in the book. The datasets required for the exercises are named in each exercise by an appropriate filename; for example, larain for the Los Angeles rainfall data. However, if you are using the TSA package, the datasets are part of the package and may be accessed through the R command data(larain), for example.

All of the datasets are also available at the textbook website as ACSCII files with variable names in the first row. We believe that many of the plots and calculations

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described in the book could also be obtained with other software, such as SAS©, Splus©, Statgraphics©, SCA©, EViews©, RATS©, Ox©, and others.

This book is a second edition of the book *Time Series Analysis* by Jonathan Cryer, published in 1986 by PWS-Kent Publishing (Duxbury Press). This new edition contains nearly all of the well-received original in addition to considerable new material, numerous new datasets, and new exercises. Some of the new topics that are integrated with the original include unit root tests, extended autocorrelation functions, subset ARIMA models, and bootstrapping. Completely new chapters cover the topics of time series regression models, time series models of heteroscedasticity, spectral analysis, and threshold models. Although the level of difficulty in these new chapters is somewhat higher than in the more basic material, we believe that the discussion is presented in a way that will make the material accessible and quite useful to a broad audience of users. Chapter 15, Threshold Models, is placed last since it is the only chapter that deals with nonlinear time series models. It could be covered earlier, say after Chapter 12. Also, Chapters 13 and 14 on spectral analysis could be covered after Chapter 10.

We would like to thank John Kimmel, Executive Editor, Statistics, at Springer, for his continuing interest and guidance during the long preparation of the manuscript. Professor Howell Tong of the London School of Economics, Professor Henghsiu Tsai of Academica Sinica, Taipei, Professor Noelle Samia of Northwestern University, Professor W. K. Li and Professor Kai W. Ng, both of the University of Hong Kong, and Professor Nils Christian Stenseth of the University of Oslo kindly read parts of the manuscript, and Professor Jun Yan used a preliminary version of the text for a class at the University of Iowa. Their constructive comments are greatly appreciated. We would like to thank Samuel Hao who helped with the exercise solutions and read the appendix: An Introduction to R. We would also like to thank several anonymous reviewers who read the manuscript at various stages. Their reviews led to a much improved book. Finally, one of the authors (JDC) would like to thank Dan, Marian, and Gene for providing such a great place, *Casa de Artes*, Club Santiago, Mexico, for working on the first draft of much of this new edition.

Iowa City, Iowa
January 2008

Jonathan D. Cryer
Kung-Sik Chan

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CHAPTER 1

INTRODUCTION

Data obtained from observations collected sequentially over time are extremely common. In business, we observe weekly interest rates, daily closing stock prices, monthly price indices, yearly sales figures, and so forth. In meteorology, we observe daily high and low temperatures, annual precipitation and drought indices, and hourly wind speeds. In agriculture, we record annual figures for crop and livestock production, soil erosion, and export sales. In the biological sciences, we observe the electrical activity of the heart at millisecond intervals. In ecology, we record the abundance of an animal species. The list of areas in which time series are studied is virtually endless. The purpose of time series analysis is generally twofold: to understand or model the stochastic mechanism that gives rise to an observed series and to predict or forecast the future values of a series based on the history of that series and, possibly, other related series or factors.

This chapter will introduce a variety of examples of time series from diverse areas of application. A somewhat unique feature of time series and their models is that we usually cannot assume that the observations arise independently from a common population (or from populations with different means, for example). Studying models that incorporate dependence is the key concept in time series analysis.

1.1 Examples of Time Series

In this section, we introduce a number of examples that will be pursued in later chapters.

Annual Rainfall in Los Angeles

Exhibit 1.1 displays a time series plot of the annual rainfall amounts recorded in Los Angeles, California, over more than 100 years. The plot shows considerable variation in rainfall amount over the years—some years are low, some high, and many are in-between in value. The year 1883 was an exceptionally wet year for Los Angeles, while 1983 was quite dry. For analysis and modeling purposes we are interested in whether or not consecutive years are related in some way. If so, we might be able to use one year's rainfall value to help forecast next year's rainfall amount. One graphical way to investigate that question is to pair up consecutive rainfall values and plot the resulting scatterplot of pairs.

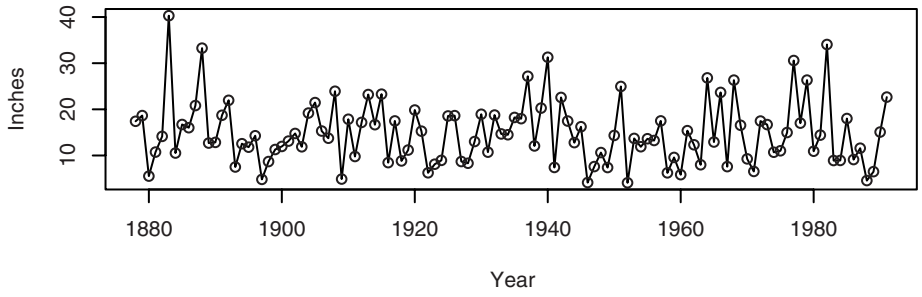
Exhibit 1.2 shows such a scatterplot for rainfall. For example, the point plotted near the lower right-hand corner shows that the year of extremely high rainfall, 40 inches in 1883, was followed by a middle of the road amount (about 12 inches) in 1884. The point

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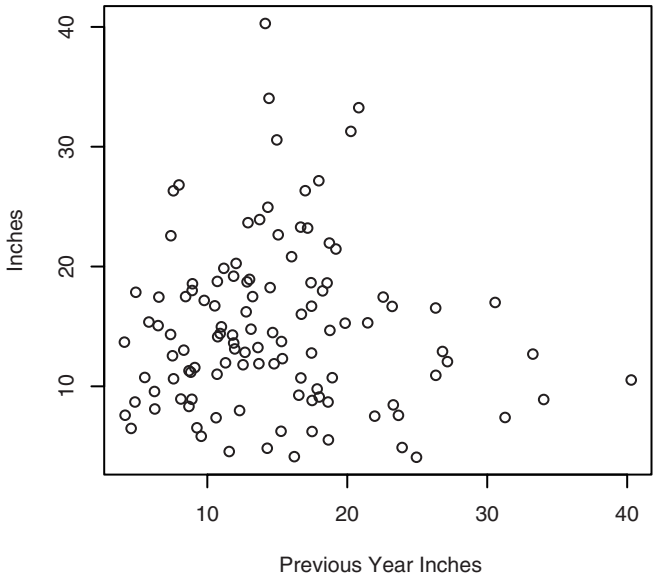
near the top of the display shows that the 40 inch year was preceded by a much more typical year of about 15 inches.

Exhibit 1.1 Time Series Plot of Los Angeles Annual Rainfall




```
> library(TSA)
> win.graph(width=4.875, height=2.5,pointsize=8)
> data(larain); plot(larain,ylab='Inches',xlab='Year',type='o')
```

Exhibit 1.2 Scatterplot of LA Rainfall versus Last Year's LA Rainfall

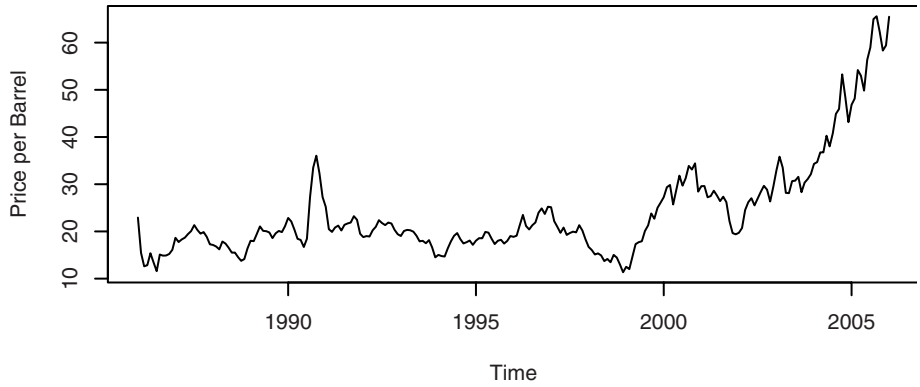



```
> win.graph(width=3,height=3,pointsize=8)
> plot(y=larain,x=zlag(larain),ylab='Inches',
    xlab='Previous Year Inches')
```

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Exhibit 5.1 Monthly Price of Oil: January 1986–January 2006




```
> win.graph(width=4.875,height=3,pointsize=8)
> data(oil.price)
> plot(oil.price, ylab='Price per Barrel',type='l')
```

5.1 Stationarity Through Differencing

Consider again the AR(1) model

$$Y_t = \phi Y_{t-1} + e_t \tag{5.1.1}$$

We have seen that assuming e_t is a true "innovation" (that is, e_t is uncorrelated with $Y_{t-1}, Y_{t-2},\ldots$), we must have $|\phi| < 1$. What can we say about solutions to Equation (5.1.1) if $|\phi| \geq 1$? Consider in particular the equation

$$Y_t = 3Y_{t-1} + e_t \tag{5.1.2}$$

Iterating into the past as we have done before yields

$$Y_t = e_t + 3e_{t-1} + 3^2 e_{t-2} + \cdots + 3^{t-1} e_1 + 3^t Y_0 \tag{5.1.3}$$

We see that the influence of distant past values of Y_t and e_t does not die out—indeed, the weights applied to Y_0 and e_1 grow exponentially large. In Exhibit 5.2, we show the values for a very short simulation of such a series. Here the white noise sequence was generated as standard normal variables and we used $Y_0 = 0$ as an initial condition.

Exhibit 5.2 Simulation of the Explosive "AR(1) Model" $Y_t = 3Y_{t-1} + e_t$

t	1	2	3	4	5	6	7	8
e_t	0.63	−1.25	1.80	1.51	1.56	0.62	0.64	−0.98
Y_t	0.63	0.64	3.72	12.67	39.57	119.33	358.63	1074.91

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8.9 The data file named robot contains a time series obtained from an industrial robot. The robot was put through a sequence of maneuvers, and the distance from a desired ending point was recorded in inches. This was repeated 324 times to form the time series. Compare the fits of an AR(1) model and an IMA(1,1) model for these data in terms of the diagnostic tests discussed in this chapter.

8.10 The data file named deere3 contains 57 consecutive values from a complex machine tool at Deere & Co. The values given are deviations from a target value in units of ten millionths of an inch. The process employs a control mechanism that resets some of the parameters of the machine tool depending on the magnitude of deviation from target of the last item produced. Diagnose the fit of an AR(1) model for these data in terms of the tests discussed in this chapter.

8.11 Exhibit 6.31 on page 139, suggested specifying either an AR(1) or possibly an AR(4) model for the difference of the logarithms of the oil price series. (The filename is oil.price).

(a) Estimate both of these models using maximum likelihood and compare the results using the diagnostic tests considered in this chapter.

(b) Exhibit 6.32 on page 140, suggested specifying an MA(1) model for the difference of the logs. Estimate this model by maximum likelihood and perform the diagnostic tests considered in this chapter.

(c) Which of the three models AR(1), AR(4), or MA(1) would you prefer given the results of parts (a) and (b)?

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It is important to remember that the local polynomial approach assumes that the true lag 1 regression function is a smooth function. If the true lag 1 regression function is discontinuous, then the local polynomial approach may yield misleading estimates. However, a sharp turn in the estimated regression function may serve as a warning that the smoothness condition may not hold for the true lag 1 regression function.

15.2 Tests for Nonlinearity

Several tests have been proposed for assessing the need for nonlinear modeling in time series analysis. Some of these tests, such as those studied by Keenan (1985), Tsay (1986), and Luukkonen et al. (1988), can be interpreted as Lagrange multiplier tests for specific nonlinear alternatives.

Keenan (1985) derived a test for nonlinearity analogous to Tukey's one degree of freedom for nonadditivity test (see Tukey, 1949). Keenan's test is motivated by approximating a nonlinear stationary time series by a second-order Volterra expansion (Wiener, 1958)

$$Y_t = \mu + \sum_{\mu=-\infty}^{\infty} \theta_\mu \varepsilon_{t-\mu} + \sum_{\nu=-\infty}^{\infty} \sum_{\mu=-\infty}^{\infty} \theta_{\mu\nu} \varepsilon_{t-\mu} \varepsilon_{t-\nu} \tag{15.2.1}$$

where $\{\varepsilon_t, -\infty < t < \infty\}$ is a sequence of independent and identically distributed zero-mean random variables. The process $\{Y_t\}$ is linear if the double sum on the right-hand side of (15.2.1) vanishes. Thus, we can test the linearity of the time series by testing whether or not the double sum vanishes. In practice, the infinite series expansion has to be truncated to a finite sum. Let $Y_1,\ldots,Y_n$ denote the observations. Keenan's test can be implemented as follows:

(i) Regress Y_t on $Y_{t-1},\ldots,Y_{t-m}$, including an intercept term, where m is some prespecified positive integer; calculate the fitted values $\{\hat{Y}_t\}$ and the residuals $\{\hat{e}_t\}$, for $t = m+1,\ldots,n$; and set $RSS = \Sigma \hat{e}_t^2$, the residual sum of squares.

(ii) Regress $\hat{Y}_t^2$ on $Y_{t-1},\ldots,Y_{t-m}$, including an intercept term, and calculate the residuals $\{\hat{\xi}_t\}$ for $t = m+1,\ldots, n$.

(iii) Regress $\hat{e}_t$ on the residuals $\hat{\xi}_t$ without an intercept for $t = m+1,\ldots, n$, and Keenan's test statistic, denoted by $\hat{F}$, is obtained by multiplying $(n-2m-2)/(n-m-1)$ to the F-statistic for testing that the last regression function is identically zero. Specifically, let

$$\eta = \eta_0 \sqrt{\sum_{t=m+1}^{n} \hat{\xi}_t^2} \tag{15.2.2}$$

where η_0 is the regression coefficient. Form the test statistic

$$\hat{F} = \frac{\eta^2 (n-2m-2)}{RSS - \eta^2} \tag{15.2.3}$$

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```
         ma1     ma2    sma1  intercept       AO    IO-63   IO-106
      0.2432  0.1729  0.0899    27.7658  37.7247  28.1777  23.2698
s.e.  0.0767  0.0698  0.0713     0.7544   5.4619   5.5982   5.5740

sigma^2 estimated as 30.67:  log likelihood = -407.06,  aic = 828.13
```

Exercise 11.19

Let us see the plot of the log-transformed weekly unit sales of lite potato chips and the weekly average price over a period of 104 weeks.

```
> library(TSA)
> data(bluebirdlite)
> ts.bluebirdlite=ts(bluebirdlite)
> plot(ts.bluebirdlite,yax.flip=T)
```

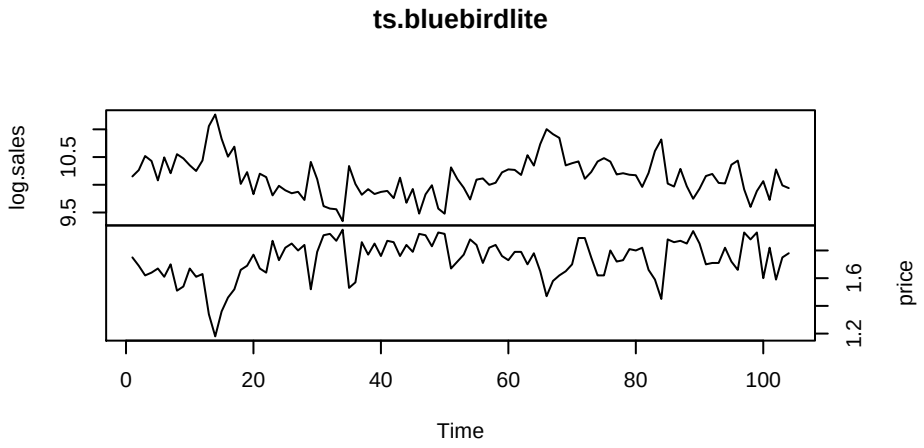


Figure 17: Weekly Log(Sales) and Price Series for Bluebirdlite Potato Chips

Next, after differencing and using prewhitened data, we draw the plot for CCF, which is significant only at lag 0, suggesting a strong contemporaneous negative relationship between lag 1 of price and sales. Higher prices are associated with lower sales.

```
> prewhiten(y=diff(ts.bluebirdlite)[,1],x=diff(ts.bluebirdlite)
+ [,2],ylab='CCF')
```


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