## Student Study and Solutions Manual



# Trigonometry 

## NINTH EDITION

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## C H A P TER P

## Prerequisites

## Section P. 1 Review of Real Numbers and Their Properties

1. irrational
2. absolute value
3. terms
4. $-9,-\frac{7}{2}, 5, \frac{2}{3}, \sqrt{2}, 0,1,-4,2,-11$
(a) Natural numbers: 5, 1, 2
(b) Whole numbers: $0,5,1,2$
(c) Integers: $-9,5,0,1,-4,2,-11$
(d) Rational numbers: $-9,-\frac{7}{2}, 5, \frac{2}{3}, 0,1,-4,2,-11$
(e) Irrational numbers: $\sqrt{2}$
5. $2.01,0.666 \ldots,-13,0.010110111 \ldots, 1,-6$
(a) Natural numbers: 1
(b) Whole numbers: 1
(c) Integers: $-13,1,-6$
(d) Rational numbers: 2.01, $0.666 \ldots,-13,1,-6$
(e) Irrational numbers: $0.010110111 \ldots$
6. (a)

(b)

(c)

(d)

7. $-4>-8$

8. $\frac{5}{6}>\frac{2}{3}$

9. (a) The inequality $x \leq 5$ denotes the set of all real numbers less than or equal to 5 .
(b)

(c) The interval is unbounded.
10. (a) The interval $[4, \infty)$ denotes the set of all real numbers greater than or equal to 4 .
(b)

(c) The interval is unbounded.
11. (a) The inequality $-2<x<2$ denotes the set of all real numbers greater than -2 and less than 2 .
(b)

(c) The interval is bounded.
12. (a) The interval $[-5,2)$ denotes the set of all real numbers greater than or equal to -5 and less than 2 .

(c) The interval is bounded.
13. $y \geq 0 ;[0, \infty)$
14. $10 \leq t \leq 22 ;[10,22]$
15. $W>65 ;(65, \infty)$
16. $|-10|=-(-10)=10$
17. $|3-8|=|-5|=-(-5)=5$
18. $|-1|-|-2|=1-2=-1$
19. $\frac{-5}{|-5|}=\frac{-5}{-(-5)}=\frac{-5}{5}=-1$
20. If $x<-2$, then $x+2$ is negative. So, $\frac{|x+2|}{x+2}=\frac{-(x+2)}{x+2}=-1$.
21. $|-4|=|4|$ because $|-4|=4$ and $|4|=4$.
22. $-|-6|<|-6|$ because $|-6|=6$ and $-|-6|=-(6)=-6$.
23. $d(126,75)=|75-126|=51$
24. $d\left(-\frac{5}{2}, 0\right)=\left|0-\left(-\frac{5}{2}\right)\right|=\frac{5}{2}$
25. $d\left(\frac{16}{5}, \frac{112}{75}\right)=\left|\frac{112}{75}-\frac{16}{5}\right|=\frac{128}{75}$
26. $d(x, 5)=|x-5|$ and $d(x, 5) \leq 3$, so $|x-5| \leq 3$.

## Receipts, R Expenditures, E $\quad|\mathbf{R}-\mathbf{E}|$

55. $\$ 1880.1 \quad \$ 2292.8$
$\mid 1880.1$ - $2292.8 \mid=\$ 412.7$ billion
56. $\$ 2524.0$
\$2982.5
$|2524.0-2982.5|=\$ 458.5$ billion
57. $7 x+4$

Terms: $7 x, 4$
Coefficient: 7
61. $4 x^{3}+\frac{x}{2}-5$

Terms: $4 x^{3}, \frac{x}{2},-5$
Coefficients: $4, \frac{1}{2}$
63. $4 x-6$
(a) $4(-1)-6=-4-6=-10$
(b) $4(0)-6=0-6=-6$
71. $x(3 y)=(x \cdot 3) y$ Associative Property of Multiplication

$$
=(3 x) y \quad \text { Commutative Property of Multiplication }
$$

73. $\frac{5}{8}-\frac{5}{12}+\frac{1}{6}=\frac{15}{24}-\frac{10}{24}+\frac{4}{24}=\frac{9}{24}=\frac{3}{8}$
74. $\frac{2 x}{3}-\frac{x}{4}=\frac{8 x}{12}-\frac{3 x}{12}=\frac{5 x}{12}$
75. (a) Because $A>0,-A<0$.

The expression is negative.
(b) Because $B<A, B-A<0$. The expression is negative.
(c) Because $C<0,-C>0$.

The expression is positive.
(d) Because $A>C, A-C>0$. The expression is positive.
65. $-x^{2}+5 x-4$
(a) $-(-1)^{2}+5(-1)-4=-1-5-4=-10$
(b) $-(1)^{2}+5(1)-4=-1+5-4=0$
67. $\frac{1}{(h+6)}(h+6)=1, h \neq-6$

Multiplicative Inverse Property
69. $2(x+3)=2 \cdot x+2 \cdot 3$

Distributive Property
79. False. Because 0 is nonnegative but not positive, not every nonnegative number is positive.
81. (a)

| $n$ | 0.0001 | 0.01 | 1 | 100 | 10,000 |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $5 / n$ | 50,000 | 500 | 5 | 0.05 | 0.0005 |

(b) (i) As $n$ approaches 0 , the value of $5 / n$ increases without bound (approaches infinity).
(ii) As $n$ increases without bound (approaches infinity), the value of $5 / n$ approaches 0 .

## Section P. 2 Solving Equations

1. equation
2. extraneous
3. $x+11=15$

$$
x+11-11=15-11
$$

$$
x=4
$$

7. $7-2 x=25$
$7-7-2 x=25-7$

$$
-2 x=18
$$

$$
\frac{-2 x}{-2}=\frac{18}{-2}
$$

$$
x=-9
$$

$$
\text { 9. } \begin{aligned}
4 y+2-5 y & =7-6 y \\
4 y-5 y+2 & =7-6 y \\
-y+2 & =7-6 y \\
-y+6 y+2 & =7-6 y+6 y \\
5 y+2 & =7 \\
5 y+2-2 & =7-2 \\
5 y & =5 \\
\frac{5 y}{5} & =\frac{5}{5} \\
y & =1
\end{aligned}
$$

11. $x-3(2 x+3)=8-5 x$

$$
\begin{aligned}
x-6 x-9 & =8-5 x \\
-5 x-9 & =8-5 x \\
-5 x+5 x-9 & =8-5 x+5 x \\
-9 & \neq 8
\end{aligned}
$$

No solution
13. $\frac{3 x}{8}-\frac{4 x}{3}=4 \quad$ or $\quad \frac{3 x}{8}-\frac{4 x}{3}=4$

$$
\begin{array}{rlrl}
\frac{9 x}{24}-\frac{32 x}{24} & =4 & 24\left(\frac{3 x}{8}-\frac{4 x}{3}\right) & =24(4) \\
-\frac{23 x}{24} & =4 & 9 x-32 x & =96 \\
-\frac{23 x}{24}\left(-\frac{24}{23}\right) & =4\left(-\frac{24}{23}\right) & -23 x & =96 \\
x & =-\frac{96}{23} & x & =-\frac{96}{23}
\end{array}
$$

15. $\quad \frac{5 x-4}{5 x+4}=\frac{2}{3}$

$$
\begin{aligned}
3(5 x-4) & =2(5 x+4) \\
15 x-12 & =10 x+8 \\
5 x & =20 \\
x & =4
\end{aligned}
$$

17. $10-\frac{13}{x}=4+\frac{5}{x}$

$$
\begin{aligned}
\frac{10 x-13}{x} & =\frac{4 x+5}{x} \\
10 x-13 & =4 x+5 \\
6 x & =18 \\
x & =3
\end{aligned}
$$

19. $\frac{x}{x+4}+\frac{4}{x+4}+2=0$

$$
\begin{array}{r}
\frac{x+4}{x+4}+2=0 \\
1+2=0 \\
3 \neq 0
\end{array}
$$

Contradiction; no solution

The second method is easier. The fractions are eliminated in the first step.
21. $\frac{2}{(x-4)(x-2)}=\frac{1}{x-4}+\frac{2}{x-2} \quad$ Multiply both sides by $(x-4)(x-2)$.

$$
\begin{aligned}
2 & =1(x-2)+2(x-4) \\
2 & =x-2+2 x-8 \\
2 & =3 x-10 \\
12 & =3 x \\
4 & =x
\end{aligned}
$$

A check reveals that $x=4$ is an extraneous solution-it makes the denominator zero. There is no real solution.
23. $\frac{1}{x-3}+\frac{1}{x+3}=\frac{10}{x^{2}-9}$

$$
\begin{aligned}
\frac{1}{x-3}+\frac{1}{x+3} & =\frac{10}{(x+3)(x-3)} \quad \text { Multiply both sides by }(x+3)(x-3) . \\
1(x+3)+1(x-3) & =10 \\
2 x & =10 \\
x & =5
\end{aligned}
$$

